9 (a) The number of people living in six houses is

$$
3, \quad 8, \quad 4, \quad x, \quad y \quad \text { and } \quad z .
$$

The median is $7 \frac{1}{2}$.
The mode is 8 .
The mean is 7 .

Find a value for each of $x, y$ and $z$.
(b) The grouped frequency table below shows the amount ( $\$ A$ ) spent on travel by a number of students.

| Cost of travel $(\$ A)$ | $0<A \leqslant 10$ | $10<A \leqslant 20$ | $20<A \leqslant 40$ |
| :---: | :---: | :---: | :---: |
| Frequency | 15 | $m$ | $n$ |

(i) Write down an estimate for the total amount in terms of $m$ and $n$.
(ii) The calculated estimate of the mean amount is $\$ 13$ exactly.

Write down an equation containing $m$ and $n$.
Show that it simplifies to $2 m+17 n=120$.
(iii) A student drew a histogram to represent this data.

The area of the rectangle representing the $0<A \leqslant 10$ group was equal to the sum of the areas of the other two rectangles.

Explain why $m+n=15$.
(iv) Find the values of $m$ and $n$ by solving the simultaneous equations

$$
\begin{gather*}
2 m+17 n=120 \\
m+n=15 \tag{3}
\end{gather*}
$$

3 The depth, $d$ centimetres, of a river was recorded each day during a period of one year (365 days). The results are shown by the cumulative frequency curve.

(a) Use the cumulative frequency curve to find
(i) the median depth,
(ii) the inter-quartile range,
(iii) the depth at the $40^{\text {th }}$ percentile,
(iv) the number of days when the depth of the river was at least 25 cm .
(b)

| $d$ | $0<d \leqslant 10$ | $10<d \leqslant 20$ | $20<d \leqslant 30$ | $30<d \leqslant 40$ | $40<d \leqslant 50$ | $50<d \leqslant 60$ | $60<d \leqslant 70$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of days | 17 | 41 | 62 | 98 | 85 | $p$ | $q$ |

(i) Show that $p=47$ and $q=15$.
(ii) Use the information in the table and the values of $p$ and $q$ to calculate an estimate of the mean depth of the river.
(c) The following information comes from the table in part (b).

| $d$ | $0<d \leqslant 20$ | $20<d \leqslant 40$ | $40<d \leqslant 70$ |
| :---: | :---: | :---: | :---: |
| Number of days | 58 | 160 | 147 |

A histogram was drawn to show this information.
The height of the column for the interval $20<d \leqslant 40$ was 8 cm .
Calculate the height of each of the other two columns.
[Do not draw the histogram.]

7 The speeds ( $v$ kilometres/hour) of 150 cars passing a $50 \mathrm{~km} / \mathrm{h}$ speed limit sign are recorded.
A cumulative frequency curve to show the results is drawn below.

(a) Use the graph to find
(i) the median speed,
(ii) the inter-quartile range of the speeds,
(iii) the number of cars travelling with speeds of more than $50 \mathrm{~km} / \mathrm{h}$.
(b) A frequency table showing the speeds of the cars is

| Speed $(v \mathrm{~km} / \mathrm{h})$ | $30<v \leqslant 35$ | $35<\nu \leqslant 40$ | $40<v \leqslant 45$ | $45<v \leqslant 50$ | $50<\nu \leqslant 55$ | $55<\nu \leqslant 60$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 10 | 17 | 33 | 42 | $n$ | 16 |

(i) Find the value of $n$.
(ii) Calculate an estimate of the mean speed.
(c) Answer this part of this question on a sheet of graph paper.

Another frequency table for the same speeds is

| Speed $(v \mathrm{~km} / \mathrm{h})$ | $30<v \leqslant 40$ | $40<v \leqslant 55$ | $55<v \leqslant 60$ |
| :---: | :---: | :---: | :---: |
| Frequency | 27 | 107 | 16 |

Draw an accurate histogram to show this information.
Use 2 cm to represent 5 units on the speed axis and 1 cm to represent 1 unit on the frequency density axis (so that $1 \mathrm{~cm}^{2}$ represents 2.5 cars).

8

$$
\mathrm{f}(x)=x^{2}-4 x+3 \quad \text { and } \quad \mathrm{g}(x)=2 x-1
$$

(a) Solve $\mathrm{f}(x)=0$.
(b) Find $\mathrm{g}^{-1}(x)$.
(c) Solve $\mathrm{f}(x)=\mathrm{g}(x)$, giving your answers correct to 2 decimal places.
(d) Find the value of $\operatorname{gf}(-2)$.
(e) Find $\operatorname{fg}(x)$. Simplify your answer.

Kristina asked 200 people how much water they drink in one day.
The table shows her results.

| Amount of water ( $x$ litres) | Number of people |
| :---: | :---: |
| $0<x \leqslant 0.5$ | 8 |
| $0.5<x \leqslant 1$ | 27 |
| $1<x \leqslant 1.5$ | 45 |
| $1.5<x \leqslant 2$ | 50 |
| $2<x \leqslant 2.5$ | 39 |
| $2.5<x \leqslant 3$ | 7 |
| $3<x \leqslant 3.5$ | 3 |
| $3.5<x \leqslant 4$ |  |

(a) Write down the modal interval.
(b) Calculate an estimate of the mean.
(c) Make a cumulative frequency table for this data.
(d) Using a scale of 4 cm to 1 litre of water on the horizontal axis and 1 cm to 10 people on the vertical axis, draw the cumulative frequency graph.
(e) Use your cumulative frequency graph to find
(i) the median,
(ii) the $40^{\text {th }}$ percentile,
(iii) the number of people who drink at least 2.6 litres of water.
(f) A doctor recommends that a person drinks at least 1.8 litres of water each day. What percentage of these 200 people do not drink enough water?


200 people record the number of hours they work in a week.
The cumulative frequency graph shows this information.
(a) Use the graph to find
(i) the median,
(ii) the upper quartile,
(iii) the inter-quartile range,
(iv) the number of people who work more than 60 hours in a week.
(b) Omar uses the graph to make the following frequency table.

| Hours <br> worked $(h)$ | $0<h \leqslant 10$ | $10<h \leqslant 20$ | $20<h \leqslant 30$ | $30<h \leqslant 40$ | $40<h \leqslant 50$ | $50<h \leqslant 60$ | $60<h \leqslant 70$ | $70<h \leqslant 80$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 12 | 34 | 36 | 30 | 38 | 30 | $p$ | $q$ |

(i) Use the graph to find the values of $p$ and $q$.
(ii) Calculate an estimate of the mean number of hours worked in a week.
(c) Shalini uses the graph to make a different frequency table.

| Hours worked ( $h$ ) | $0<h \leqslant 30$ | $30<h \leqslant 40$ | $40<h \leqslant 50$ | $50<h \leqslant 80$ |
| :---: | :---: | :---: | :---: | :---: |
| Frequency | 82 | 30 | 38 | 50 |

When she draws a histogram, the height of the column for the interval $30<h \leqslant 40$ is 9 cm .

Calculate the height of each of the other three columns.

2 A normal die, numbered 1 to 6 , is rolled 50 times.

The results are shown in the frequency table.


| Score | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 15 | 10 | 7 | 5 | 6 | 7 |

(a) Write down the modal score.

Answer(a)
(b) Find the median score.
(c) Calculate the mean score.
(d) The die is then rolled another 10 times.

The mean score for the 60 rolls is 2.95 .
Calculate the mean score for the extra 10 rolls.

9 The heights of 100 students are measured.
The results have been used to draw this cumulative frequency diagram.

(a) Find
(i) the median height,
(ii) the lower quartile,
(iii) the inter-quartile range,

> Answer(a)(iii)
(iv) the number of students with a height greater than 177 cm .

Answer(a)(iv)
(b) The frequency table shows the information about the 100 students who were measured.

| Height $(h \mathrm{~cm})$ | $150<h \leqslant 160$ | $160<h \leqslant 170$ | $170<h \leqslant 180$ | $180<h \leqslant 190$ |
| :---: | :---: | :---: | :---: | :---: |
| Frequency |  |  | 47 | 18 |

(i) Use the cumulative frequency diagram to complete the table above.
(ii) Calculate an estimate of the mean height of the 100 students.

240 students are asked about the number of people in their families.
The table shows the results.

| Number of people in family | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 1 | 1 | 17 | 12 | 6 | 3 |

(a) Find
(i) the mode,

> Answer(a)(i)
(ii) the median,
Answer(a)(ii)
(iii) the mean.

> Answer(a)(iii)
(b) Another $n$ students are asked about the number of people in their families.

The mean for these $n$ students is 3 .
Find, in terms of $n$, an expression for the mean number for all $(40+n)$ students.

6 The masses of 60 potatoes are measured.
The table shows the results.

| Mass ( $m$ grams) | $10<m \leqslant 20$ | $20<m \leqslant 40$ | $40<m \leqslant 50$ |
| :---: | :---: | :---: | :---: |
| Frequency | 10 | 30 | 20 |

(a) Calculate an estimate of the mean.

Answer(a) g
(b) On the grid, draw an accurate histogram to show the information in the table.


200 students were asked how many hours they exercise each week.
The table shows the results.

| Time ( $t$ hours) | $0<t \leqslant 5$ | $5<t \leqslant 10$ | $10<t \leqslant 15$ | $15<t \leqslant 20$ | $20<t \leqslant 25$ | $25<t \leqslant 30$ | $30<t \leqslant 35$ | $35<t \leqslant 40$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of <br> students | 12 | 15 | 23 | 30 | 40 | 35 | 25 | 20 |

(a) Calculate an estimate of the mean.

Answer (a).
h [4]

Use the information in the table above to complete the cumulative frequency table.
(b)

| Time ( $t$ hours) | $t \leqslant 5$ | $t \leqslant 10$ | $t \leqslant 15$ | $t \leqslant 20$ | $t \leqslant 25$ | $t \leqslant 30$ | $t \leqslant 35$ | $t \leqslant 40$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cumulative frequency | 12 | 27 | 50 | 80 | 120 |  |  | 200 |


(c) On the grid, draw a cumulative frequency diagram to show the information in the table in part (b).
(d) On your cumulative frequency diagram show how to find the lower quartile.
(e) Use your cumulative frequency diagram to find
(i) the median,
Answer(e)(i)
(ii) the inter-quartile range,
Answer(e)(ii)
(iii) the 64th percentile,

> Answer(e)(iii)
(iv) the number of students who exercise for more than 17 hours.

7 (a) The table shows how many books were borrowed by the 126 members of a library group in a month.

| Number of books | 11 | 12 | 13 | 14 | 15 | 16 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of members <br> (frequency) | 35 | 28 | 22 | 18 | 14 | 9 |

Find the mode, the median and the mean for the number of books borrowed.

(b) The 126 members record the number of hours they read in one week.

The histogram shows the results.
Frequency density


7 (a) A group of students sat an examination. Each student got one of the grades $A, B, C$ or $D$. The pie chart shows these results.


## NOT TO SCALE

36 students got grade A, shown by an angle of $108^{\circ}$.
(i) Calculate the total number of students who sat the examination.
(ii) How many students did not get grade $A$ ?
(iii) The ratio of the number of students getting grades $B, C$ or $D$ is $4: 5: 3$.

Find the number of students getting each grade.
(iv) Work out the angles in the pie chart for grades $B, C$ and $D$.
(v) Find the ratio, in its lowest terms, the number of students with grade $A$ : the number of students with grade $B$.
(b) A group of children were asked how much money they had saved. The histogram and table show the results.


| Money saved (\$m) | $0<m \leqslant 20$ | $20<m \leqslant 30$ | $30<m \leqslant 40$ | $40<m \leqslant 70$ |
| :---: | :---: | :---: | :---: | :---: |
| Frequency | 25 | $p$ | $q$ | $r$ |

Use the histogram to calculate the values of $p, q$ and $r$.

## 8 Answer the whole of this question on a sheet of graph paper.

120 passengers on an aircraft had their baggage weighed. The results are shown in the table.

| Mass of baggage $(M \mathrm{~kg})$ | $0<M \leqslant 10$ | $10<M \leqslant 15$ | $15<M \leqslant 20$ | $20<M \leqslant 25$ | $25<M \leqslant 40$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of passengers | 12 | 32 | 28 | 24 | 24 |

(a) (i) Write down the modal class.
(ii) Calculate an estimate of the mean mass of baggage for the 120 passengers. Show all your working.
(iii) Sophia draws a pie chart to show the data. What angle should she have in the $0<M \leqslant 10$ sector?
(b) Using a scale of 2 cm to represent 5 kg , draw a horizontal axis for $0<M \leqslant 40$.

Using an area scale of $1 \mathrm{~cm}^{2}$ to represent 1 passenger, draw a histogram for this data.

6 (a) Students are given marks $0,1,2,3$ or 4 for a piece of work. The table shows the number of students getting each mark.

| Mark | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 3 | 10 | 12 | 9 | $x$ |

(i) The mean mark is 2.125 .

Find the value of $x$.
(ii) Write down the lower quartile mark.
(b) The heights ( $h$ centimetres) of flowers in a shop are shown in the histogram below. All the flowers are less than 60 cm high.
One bar has not been drawn on the histogram.

Frequency density

(i) There are 25 flowers in the interval $20<h \leqslant 25$.

How many flowers are there in the intervals
(a) $25<h \leqslant 30$,
(b) $10<h \leqslant 20$ ?
(ii) There are 42 flowers in the interval $30<h \leqslant 60$.

This can be shown by a single bar on the histogram.
Calculate the height of this bar.
(iii) Calculate an estimate of the mean height of the flowers.

Answer the whole of this question on one sheet of graph paper.
The heights $(h \mathrm{~cm})$ of 270 students in a school are measured and the results are shown in the table.

| $h$ | Frequency |
| :---: | :---: |
| $120<h \leqslant 130$ | 15 |
| $130<h \leqslant 140$ | 24 |
| $140<h \leqslant 150$ | 36 |
| $150<h \leqslant 160$ | 45 |
| $160<h \leqslant 170$ | 50 |
| $170<h \leqslant 180$ | 43 |
| $180<h \leqslant 190$ | 37 |
| $190<h \leqslant 200$ | 20 |

(a) Write down the modal group.
(b) (i) Calculate an estimate of the mean height.
(ii) Explain why the answer to part (b)(i) is an estimate.
(c) The following table shows the cumulative frequencies for the heights of the students.

| $h$ | Cumulative frequency |
| :---: | :---: |
| $h \leqslant 120$ | 0 |
| $h \leqslant 130$ | $p$ |
| $h \leqslant 140$ | $q$ |
| $h \leqslant 150$ | $r$ |
| $h \leqslant 160$ | 120 |
| $h \leqslant 170$ | 170 |
| $h \leqslant 180$ | 213 |
| $h \leqslant 190$ | 250 |
| $h \leqslant 200$ | 270 |

Write down the values of $p, q$ and $r$.
(d) Using a scale of 1 cm to 5 units, draw a horizontal $h$-axis, starting at $h=120$.

Using a scale of 1 cm to 20 units on the vertical axis, draw a cumulative frequency diagram.
(e) Use your diagram to find
(i) the median height,
(ii) the upper quartile,
(iii) the inter-quartile range,
(iv) the 60th percentile.
(f) All the players in the school's basketball team are chosen from the 30 tallest students. Use your diagram to find the least possible height of any player in the basketball team.

7 (a) The quiz scores of a class of $n$ students are shown in the table.

| Quiz score | 6 | 7 | 8 | 9 |
| :--- | :--- | :--- | :--- | :--- |
| Frequency (number of students) | 9 | 3 | $a$ | 5 |

The mean score is 7.2. Find
(i) $a$,
(ii) $n$,
(iii) the median score.
(b) 200 students take a mathematics test.

The cumulative frequency diagram shows the results.


Write down
(i) the median mark,
(ii) the lower quartile,
(iii) the upper quartile,
(iv) the inter-quartile range,
(v) the lowest possible mark scored by the top 40 students,
(vi) the number of students scoring more than 25 marks.
(c) Another group of students takes an English test. The results are shown in the histogram.


100 students score marks in the range $50<x \leqslant 75$.
(i) How many students score marks in the range $0<x \leqslant 50$ ?
(ii) How many students score marks in the range $75<x \leqslant 100$ ?
(iii) Calculate an estimate of the mean mark of this group of students.

| Grade | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of students | 1 | 2 | 4 | 7 | 4 | 8 | 2 |

The table shows the grades gained by 28 students in a history test.
(i) Write down the mode.
(ii) Find the median.
(iii) Calculate the mean.
(iv) Two students are chosen at random.

Calculate the probability that they both gained grade 5 .
(v) From all the students who gained grades 4 or 5 or 6 or 7 , two are chosen at random.

Calculate the probability that they both gained grade 5 .
(vi) Students are chosen at random, one by one, from the original 28 , until the student chosen has a grade 5 .

Calculate the probability that this is the third student chosen.
(b) Claude goes to school by bus.

The probability that the bus is late is 0.1 .
If the bus is late, the probability that Claude is late to school is 0.8 .
If the bus is not late, the probability that Claude is late to school is 0.05 .
(i) Calculate the probability that the bus is late and Claude is late to school.
(ii) Calculate the probability that Claude is late to school.
(iii) The school term lasts 56 days.

How many days would Claude expect to be late?

6 (a) Each student in a class is given a bag of sweets.

The students note the number of sweets in their bag.
The results are shown in the table, where $0 \leqslant x<10$.

| Number of sweets | 30 | 31 | 32 |
| :---: | :---: | :---: | :---: |
| Frequency (number of bags) | 10 | 7 | $x$ |

(i) State the mode.
(ii) Find the possible values of the median.
(iii) The mean number of sweets is 30.65 .

Find the value of $x$.
(b) The mass, $m$ grams, of each of 200 chocolates is noted and the results are shown in the table.

| Mass ( $m$ grams) | $10<m \leqslant 20$ | $20<m \leqslant 22$ | $22<m \leqslant 24$ | $24<m \leqslant 30$ |
| :---: | :---: | :---: | :---: | :---: |
| Frequency | 35 | 115 | 26 | 24 |

(i) Calculate an estimate of the mean mass of a chocolate.
(ii) On a histogram, the height of the column for the $20<m \leqslant 22$ interval is 11.5 cm .

Calculate the heights of the other three columns.
Do not draw the histogram.

8 Fifty students are timed when running one kilometre.
The results are shown in the table.

| Time <br> $(t$ minutes $)$ | $4.0<t \leqslant 4.5$ | $4.5<t \leqslant 5.0$ | $5.0<t \leqslant 5.5$ | $5.5<t \leqslant 6.0$ | $6.0<t \leqslant 6.5$ | $6.5<t \leqslant 7.0$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 2 | 7 | 8 | 18 | 10 | 5 |

(a) Write down the modal time interval.

Answer (a) min
(b) Calculate an estimate of the mean time.

Answer(b)
min
(c)

A new frequency table is made from the results shown in the table above.

| Time <br> $(t$ minutes $)$ | $4.0<t \leqslant 5.5$ | $5.5<t \leqslant 6.0$ | $6.0<t \leqslant 7.0$ |
| :--- | :---: | :---: | :---: |
| Frequency |  | 18 |  |

(i) Complete the table by filling in the two empty boxes.
(ii) On the grid below, complete an accurate histogram to show the information in this new table.

(iii) Find the number of students represented by $1 \mathrm{~cm}^{2}$ on the histogram.

5 The cumulative frequency table shows the distribution of heights, $h$ centimetres, of 200 students.

| Height $(h \mathrm{~cm})$ | $\leqslant 130$ | $\leqslant 140$ | $\leqslant 150$ | $\leqslant 160$ | $\leqslant 165$ | $\leqslant 170$ | $\leqslant 180$ | $\leqslant 190$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cumulative frequency | 0 | 10 | 50 | 95 | 115 | 145 | 180 | 200 |

(a) Draw a cumulative frequency diagram to show the information in the table.

(b) Use your diagram to find
(i) the median,
$\qquad$
(ii) the upper quartile,
Answer(b)(ii) ................................................. cm
(iii) the interquartile range.
Answer(b)(iii) ....................................... cm
(c) (i) One of the 200 students is chosen at random.

Use the table to find the probability that the height of this student is greater than 170 cm .
(ii) One of the 200 students is chosen at random and then a second student is chosen at random from the remaining students.

Calculate the probability that one has a height greater than 170 cm and the other has a height of 140 cm or less.
Give your answer as a fraction.

Answer(c)(ii)
(d) (i) Complete this frequency table which shows the distribution of the heights of the 200 students.

| Height $(h \mathrm{~cm})$ | $130<h \leqslant 140$ | $140<h \leqslant 150$ | $150<h \leqslant 160$ | $160<h \leqslant 165$ | $165<h \leqslant 170$ | $170<h \leqslant 180$ | $180<h \leqslant 190$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 10 | 40 | 45 | 20 |  |  |  |

(ii) Complete this histogram to show the distribution of the heights of the 200 students.


380 boys each had their mass, $m$ kilograms, recorded.
The cumulative frequency diagram shows the results.

(a) Find
(i) the median,
$\qquad$
(ii) the lower quartile,
Answer(a)(ii) ......................................................
(iii) the interquartile range.
Answer(a)(iii) ........................................... kg
(b) How many boys had a mass greater than 60 kg ?
(c) (i) Use the cumulative frequency graph to complete this frequency table.

| Mass, $m$ | Frequency |
| :---: | :---: |
| $30<m \leqslant 40$ | 8 |
| $40<m \leqslant 50$ |  |
| $50<m \leqslant 60$ | 14 |
| $60<m \leqslant 70$ | 22 |
| $70<m \leqslant 80$ |  |
| $80<m \leqslant 90$ | 10 |

(ii) Calculate an estimate of the mean mass.

10 (a) For a set of six integers, the mode is 8 , the median is 9 and the mean is 10 .
The smallest integer is greater than 6 and the largest integer is 16 .
Find the two possible sets of six integers.

Answer(a) First set Second set ......... , ......... , ......... , ......... , ......... , ......... ......... , ......... , ........ , ........ , ......... , .........
(b) One day Ahmed sells 160 oranges.

He records the mass of each orange.
The results are shown in the table.

| Mass ( $m$ grams) | $50<m \leqslant 80$ | $80<m \leqslant 90$ | $90<m \leqslant 100$ | $100<m \leqslant 120$ | $120<m \leqslant 150$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequency | 30 | 35 | 40 | 40 | 15 |

(i) Calculate an estimate of the mean mass of the 160 oranges.
(ii) On the grid, complete the histogram to show the information in the table.


