## I.G.C.S.E. Geometry

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## Question 1

Use a ruler and a protractor only to draw a full size diagram and measure the sides marked with letters.


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Solution to question 1


By drawing accurate diagrams using a protractor and ruler only and measuring the sides with a ruler we have
$a=6.2 \mathrm{~cm}$
$b=4.6 \mathrm{~cm}$
$c=3.3 \mathrm{~cm}$
$d=3.2 \mathrm{~cm}$

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## Question 2

Construct the triangles below using a ruler and compass only and measure angles marked with letters.


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## Solution to question 2



By drawing accurate diagrams using a compass and ruler only and measuring the angles with a protractor we have

$$
\begin{aligned}
& a=94^{\circ} \\
& b=120^{\circ}
\end{aligned}
$$

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## Question 3

Draw a net to make a cube and mark on where you would mark on the numbers to make a die.

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Solution to question 3


There are other possibilities.
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## Question 4

Find the angles marked with letters


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Solution to question 4


Angles at a point add up to $360^{\circ}$

$$
\begin{aligned}
120^{\circ}+110^{\circ}+a+a & =360^{\circ} \\
230^{\circ}+2 a & =360^{\circ} \\
2 a & =360^{\circ}-230^{\circ} \\
2 a & =130^{\circ} \\
a & =\frac{130^{\circ}}{2}=65^{\circ}
\end{aligned}
$$



Angles on a straight line add up to $180^{\circ}$

$$
\begin{aligned}
90^{\circ}+b+2 b & =180^{\circ} \\
90^{\circ}+3 b & =180^{\circ} \\
3 b & =180^{\circ}-90^{\circ} \\
3 b & =90^{\circ} \\
b & =\frac{90^{\circ}}{3}=30^{\circ}
\end{aligned}
$$

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## Question 5

Find the angles marked with letters


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## Solution to question 5



The exterior angle of a triangle is equal to the sum of the two opposite interior angles

$$
\begin{aligned}
a+30^{\circ} & =50^{\circ} \\
a & =50^{\circ}-30^{\circ}=20^{\circ}
\end{aligned}
$$



The triangle is isosceles and therefore has two equal sides and angles.
$c=65^{\circ}$ equal base angles.

Angles in a triangle add up to $180^{\circ}$

$$
\begin{aligned}
b+65^{\circ}+65^{\circ} & =180^{\circ} \\
b+130^{\circ} & =180^{\circ} \\
b & =180^{\circ}-130^{\circ}=50^{\circ}
\end{aligned}
$$

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## Question 6

1. Find the angles marked with letters.


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Solution to question 6

$a=75^{\circ}$ (alternate angles).

$$
\begin{aligned}
62^{\circ}+b & =180^{\circ} \quad \text { (allied angles) } \\
b & =180^{\circ}-62^{\circ}=118^{\circ}
\end{aligned}
$$


$c=57^{\circ}$ (alternate angles).

$$
\begin{array}{r}
120^{\circ}+d=180^{\circ} \quad \text { (allied angles) } \\
d=180^{\circ}-120^{\circ}=60^{\circ} \\
c+d+e=180^{\circ} \quad \text { (angles on a } \\
57^{\circ}+60^{\circ}+e=180^{\circ} \quad \text { straight line) } \\
117^{\circ}+e=180^{\circ} \\
e=180^{\circ}-117^{\circ}=63^{\circ}
\end{array}
$$

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## Question 7

Find the angles marked with letters.


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## Solution to question 7

Quadrilateral


Angles in a quadrilateral add up to 360

$$
\begin{aligned}
60^{\circ}+45^{\circ}+110^{\circ}+a & =360^{\circ} \\
215^{\circ}+a & =360^{\circ} \\
a & =360^{\circ}-215^{\circ}=145^{\circ}
\end{aligned}
$$

## Regular Pentagon



Angles at a point add up to 360
$b=\frac{360^{\circ}}{5}=72^{\circ}$

Triangle $A O B$ is isosceles hence

$$
\begin{aligned}
b+c+c & =180^{\circ} \\
72^{\circ}+2 c & =180^{\circ} \\
2 c & =180^{\circ}-72^{\circ} \\
c & =\frac{108^{\circ}}{2}=54^{\circ}
\end{aligned}
$$

$$
\begin{aligned}
d & =2 c \\
& =2 \times 54^{\circ} \\
& =108^{\circ}
\end{aligned}
$$

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## Question 8

Find the angles marked in the diagram


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## Solution to question 8



Angles on a straight line add up to $180^{\circ}$

$$
\begin{aligned}
a+35^{\circ} & =180^{\circ} \\
a & =180^{\circ}-35^{\circ}=145^{\circ} \\
b+50^{\circ} & =180^{\circ} \\
b & =180^{\circ}-50^{\circ}=130^{\circ} \\
c+55^{\circ} & =180^{\circ} \\
c & =180^{\circ}-55^{\circ}=125^{\circ}
\end{aligned}
$$

The sum of the exterior angles of any polygon is $360^{\circ}$

$$
\begin{aligned}
90^{\circ}+55^{\circ}+35^{\circ}+50^{\circ}+60^{\circ}+d & =360^{\circ} \\
290^{\circ}+d & =360^{\circ} \\
d & =360^{\circ}-290^{\circ}=70^{\circ}
\end{aligned}
$$

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Question 9

Each exterior angle of a regular polygon is $30^{\circ}$. Find:
a. the number of sides of the polygon;
b. the size of each interior angle.

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## Solution to question 9

a. The sum of the exterior angles of any polygon is $360^{\circ}$

Number of sides $=\frac{360^{\circ}}{30^{\circ}}=12$ sides
b. The sum of the exterior and interior angle of any polygon is $180^{\circ}$

$$
\begin{aligned}
& e+i=180^{\circ} \\
& 30^{\circ}+i=180^{\circ} \\
& i=180^{\circ}-30^{\circ}=150^{\circ}
\end{aligned}
$$

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Question 10
Find the value of the angle $a$.


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Solution to question 10


The angle a semi-circle is a right angle.
Therefore $a+2 a=90^{\circ}$

$$
\begin{aligned}
3 a & =90^{\circ} \\
a & =\frac{90^{\circ}}{3}=30^{\circ}
\end{aligned}
$$

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