

ADDITIONAL MATHEMATICS

2002 – 2011

CLASSIFIED COORDINATE GEOMETRY

**Compiled & Edited
By**

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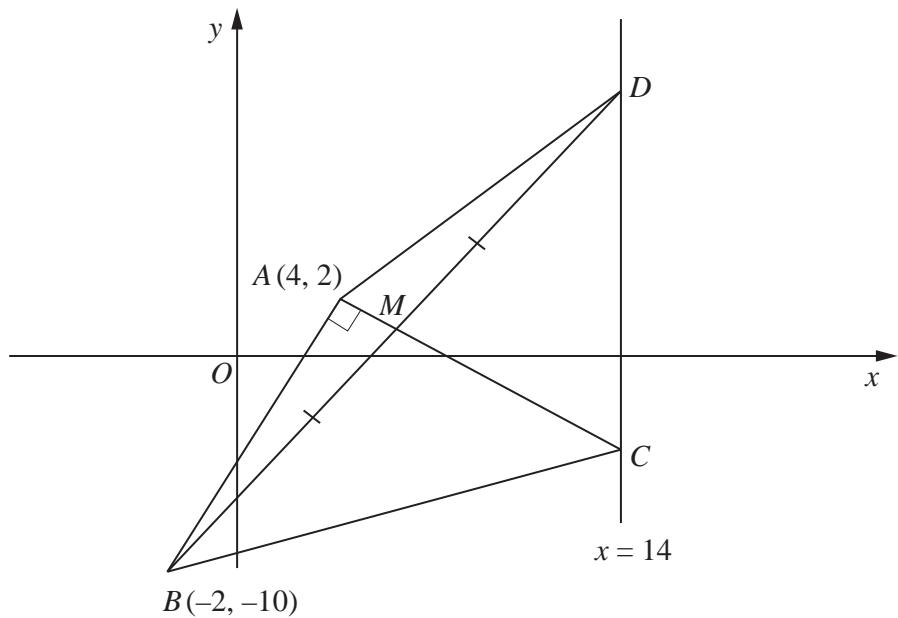
**First Edition
2011**

- 7 The points A and B have coordinates $(-2, 15)$ and $(3, 5)$ respectively. The perpendicular to the line AB at the point A $(-2, 15)$ crosses the y -axis at the point C . Find the area of the triangle ABC .

[6]

*For
Examiner's
Use*

9 Solutions to this question by accurate drawing will not be accepted.



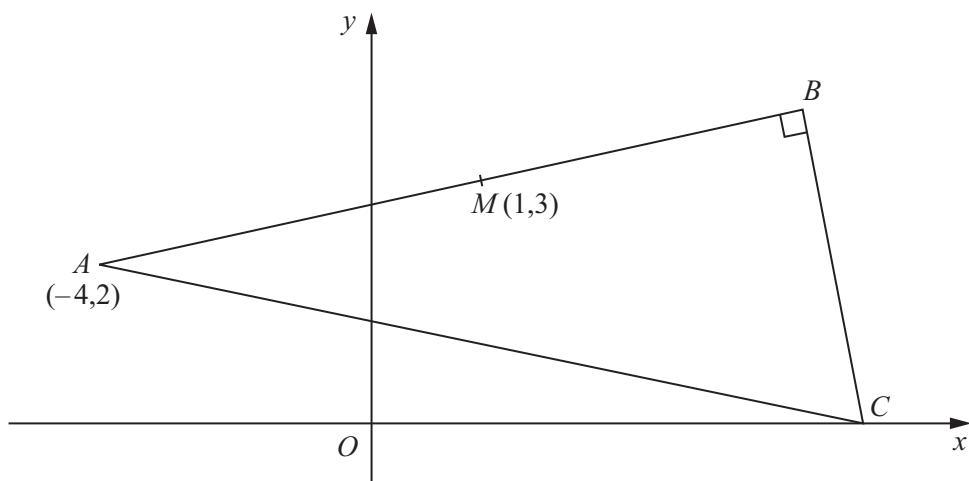
The diagram shows the quadrilateral $ABCD$ in which A is the point $(4, 2)$ and B is the point $(-2, -10)$. The points C and D lie on the line $x = 14$. The diagonal AC is perpendicular to AB and passes through the mid-point, M , of the diagonal BD . Find the area of the quadrilateral $ABCD$.

[9]

- 8 The line CD is the perpendicular bisector of the line joining the point $A (-1, -5)$ and the point $B (5, 3)$.

(i) Find the equation of the line CD .

[4]



The figure shows a right-angled triangle ABC , where the point A has coordinates $(-4, 2)$, the angle B is 90° and the point C lies on the x -axis. The point $M(1, 3)$ is the midpoint of AB . Find the area of the triangle ABC . [7]

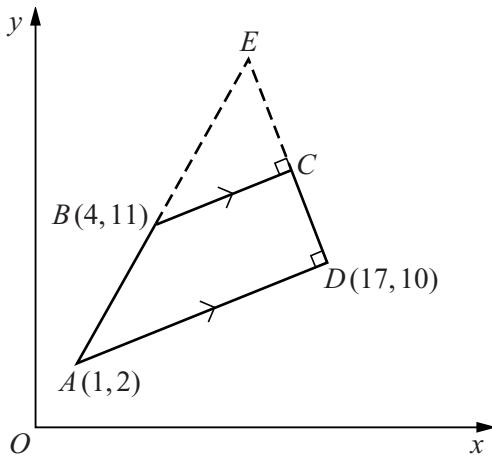
6 Solutions to this question by accurate drawing will not be accepted.

The points $A(1, 4)$, $B(3, 8)$, $C(13, 13)$ and D are the vertices of a trapezium in which AB is parallel to DC and angle BAD is 90° . Find the coordinates of D .

*For
Examiner's
Use*

[6]

Solutions to this question by accurate drawing will not be accepted.



The diagram, which is not drawn to scale, shows a trapezium $ABCD$ in which BC is parallel to AD . The side AD is perpendicular to DC . Point A is $(1, 2)$, B is $(4, 11)$ and D is $(17, 10)$. Find

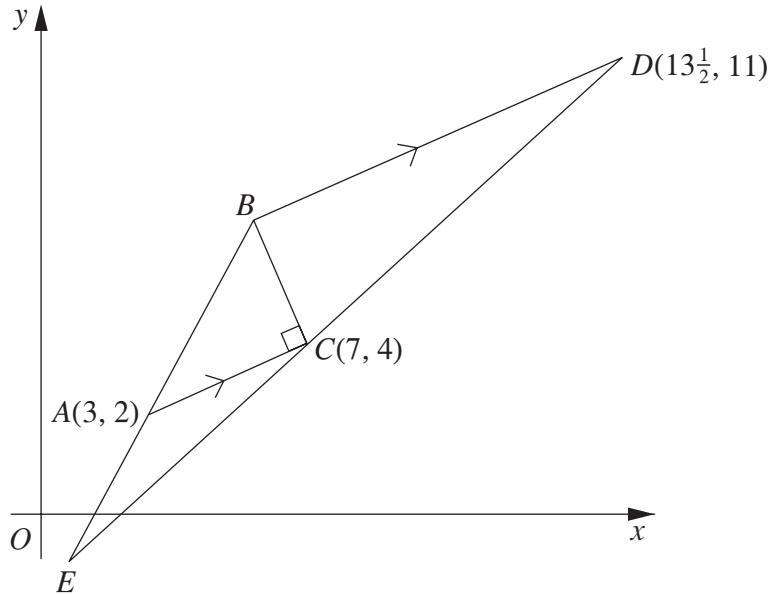
- (i) the coordinates of C .

The lines AB and DC are extended to meet at E . Find

- (ii) the coordinates of E ,
(iii) the ratio of the area of triangle EBC to the area of trapezium $ABCD$.

[11]

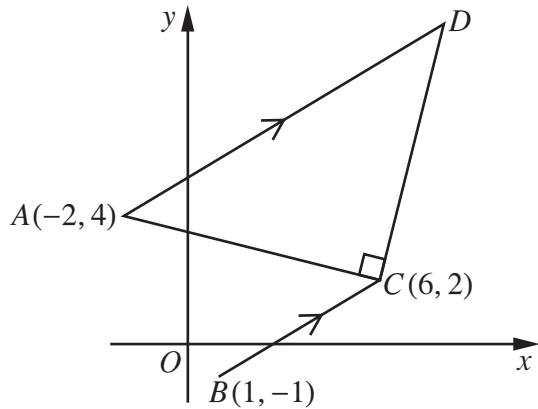
Solutions to this question by accurate drawing will not be accepted.



The diagram shows a triangle ABC in which A is the point $(3, 2)$, C is the point $(7, 4)$ and angle $ACB = 90^\circ$. The line BD is parallel to AC and D is the point $(13\frac{1}{2}, 11)$. The lines BA and DC are extended to meet at E . Find

- (i) the coordinates of B , [7]
- (ii) the ratio of the area of the quadrilateral $ABDC$ to the area of the triangle EBD . [3]

10 Solutions to this question by accurate drawing will not be accepted.



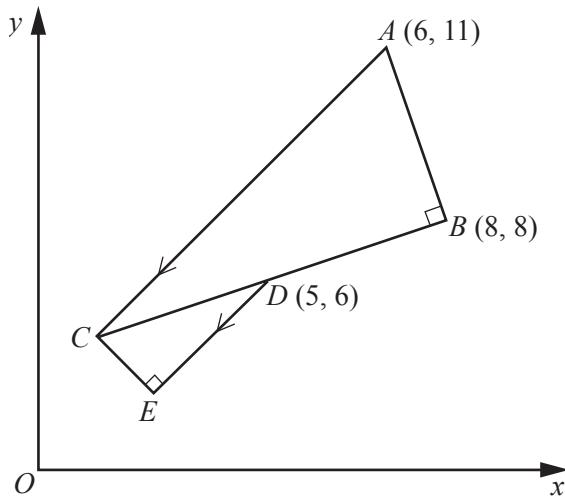
In the diagram the points A , B and C have coordinates $(-2, 4)$, $(1, -1)$ and $(6, 2)$ respectively. The line AD is parallel to BC and angle $ACD = 90^\circ$.

- (i) Find the equations of AD and CD . [6]
- (ii) Find the coordinates of D . [2]
- (iii) Show that triangle ACD is isosceles. [2]

12 Answer only **one** of the following two alternatives.

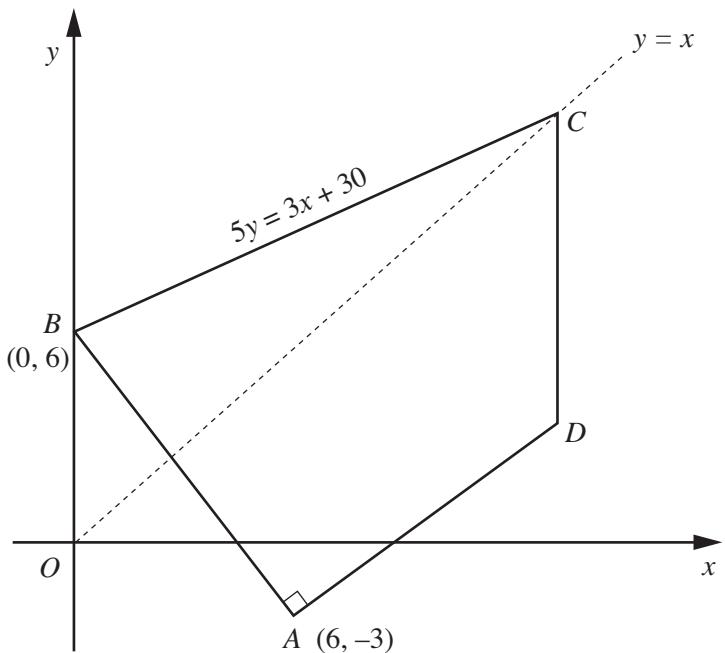
EITHER

Solutions to this question by accurate drawing will not be accepted.



The diagram, which is not drawn to scale, shows a right-angled triangle ABC , where A is the point $(6, 11)$ and B is the point $(8, 8)$.

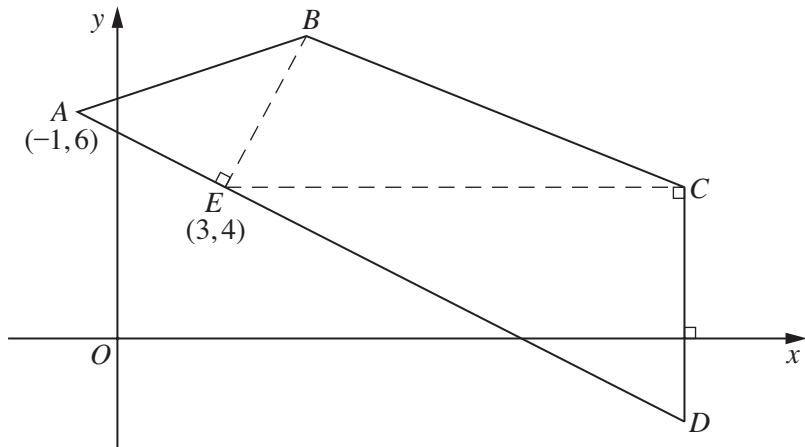
The point $D(5, 6)$ is the mid-point of BC . The line DE is parallel to AC and angle DEC is a right-angle. Find the area of the entire figure $ABDECA$. [11]



The diagram, which is not drawn to scale, shows a quadrilateral $ABCD$ in which A is $(6, -3)$, B is $(0, 6)$ and angle BAD is 90° . The equation of the line BC is $5y = 3x + 30$ and C lies on the line $y = x$. The line CD is parallel to the y -axis.

- (i) Find the coordinates of C and of D . [6]
- (ii) Show that triangle BAD is isosceles and find its area. [4]

Solutions to this question by accurate drawing will not be accepted.



The diagram shows a quadrilateral $ABCD$. The point E lies on AD such that angle $AEB = 90^\circ$. The line EC is parallel to the x -axis and the line CD is parallel to the y -axis. The points A and E are $(-1, 6)$ and $(3, 4)$ respectively. Given that the gradient of AB is $\frac{1}{3}$,

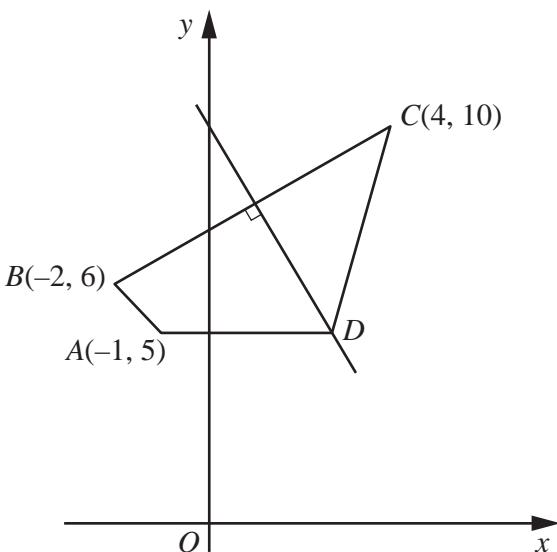
- (i) find the coordinates of B . [5]

Given also that the area of triangle EBC is 24 units 2 ,

- (ii) find the coordinates of C , [3]

- (iii) find the coordinates of D . [2]

7 Solutions to this question by accurate drawing will not be accepted.



In the diagram the points $A(-1, 5)$, $B(-2, 6)$, $C(4, 10)$ and D are the vertices of a quadrilateral in which AD is parallel to the x -axis. The perpendicular bisector of BC passes through D . Find the area of the quadrilateral $ABCD$. [8]

- 7 The points A and B have coordinates $(-2, 15)$ and $(3, 5)$ respectively. The perpendicular to the line AB at the point A $(-2, 15)$ crosses the y -axis at the point C . Find the area of the triangle ABC .

[6]

*For
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Use*

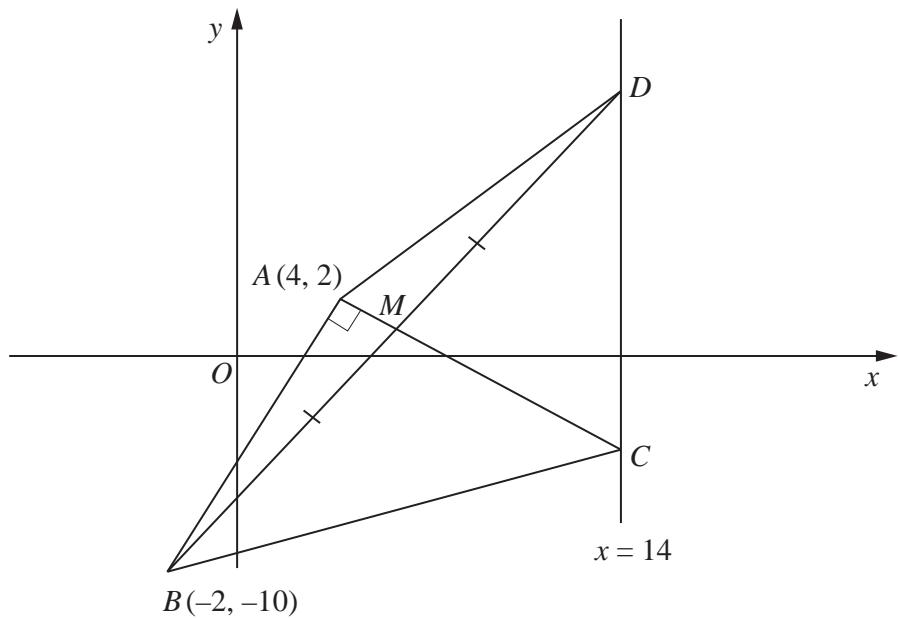
- 12 The tangent to the curve $y = 3x^3 + 2x^2 - 5x + 1$ at the point where $x = -1$ meets the y -axis at the point A .

(i) Find the coordinates of the point A . [3]

The curve meets the y -axis at the point B . The normal to the curve at B meets the x -axis at the point C . The tangent to the curve at the point where $x = -1$ and the normal to the curve at B meet at the point D .

(ii) Find the area of the triangle ACD . [7]

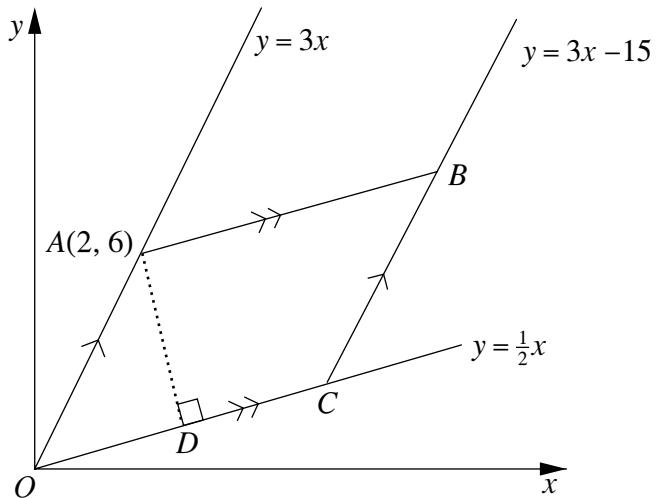
- 9** Solutions to this question by accurate drawing will not be accepted.



The diagram shows the quadrilateral $ABCD$ in which A is the point $(4, 2)$ and B is the point $(-2, -10)$. The points C and D lie on the line $x = 14$. The diagonal AC is perpendicular to AB and passes through the mid-point, M , of the diagonal BD . Find the area of the quadrilateral $ABCD$.

[9]

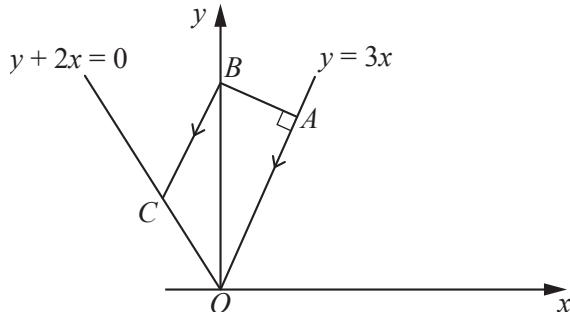
11 Solutions to this question by accurate drawing will not be accepted.



The diagram, which is not drawn to scale, shows a parallelogram $OABC$ where O is the origin and A is the point $(2, 6)$. The equations of OA , OC and CB are $y = 3x$, $y = \frac{1}{2}x$ and $y = 3x - 15$ respectively. The perpendicular from A to OC meets OC at the point D . Find

- (i) the coordinates of C , B and D , [8]
(ii) the perimeter of the parallelogram $OABC$, correct to 1 decimal place. [3]

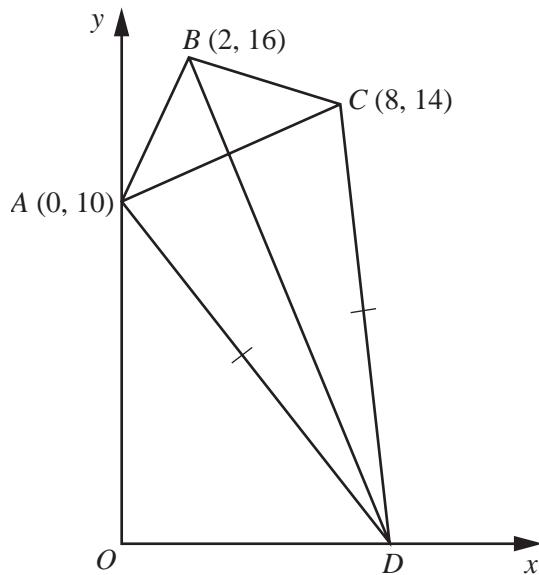
11



The diagram shows a trapezium $OABC$, where O is the origin. The equation of OA is $y = 3x$ and the equation of OC is $y + 2x = 0$. The line through A perpendicular to OA meets the y -axis at B and BC is parallel to AO . Given that the length of OA is $\sqrt{250}$ units, calculate the coordinates of A , of B and of C .

[10]

10 Solutions to this question by accurate drawing will not be accepted.



The diagram, which is not drawn to scale, shows a quadrilateral $ABCD$ in which A is $(0, 10)$, B is $(2, 16)$ and C is $(8, 14)$.

- (i) Show that triangle ABC is isosceles.

[2]

The point D lies on the x -axis and is such that $AD = CD$. Find

- (ii) the coordinates of D ,

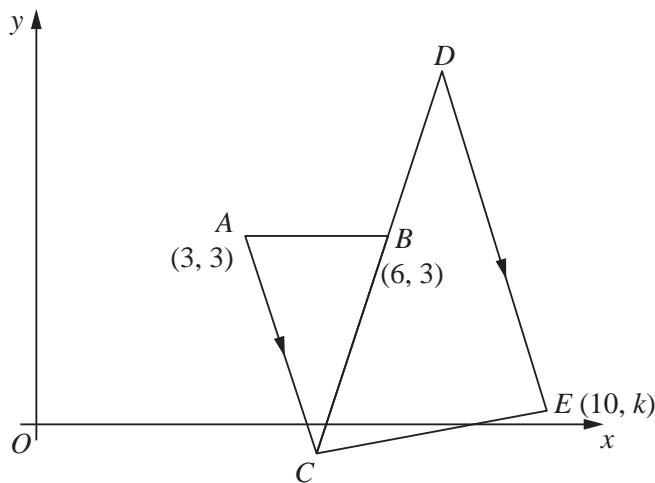
[4]

- (iii) the ratio of the area of triangle ABC to the area of triangle ACD .

[3]

OR

Solutions to this question by accurate drawing will not be accepted.



The diagram shows an isosceles triangle ABC in which A is the point $(3, 3)$, B is the point $(6, 3)$ and C lies below the x -axis. Given that the area of triangle ABC is 6 square units,

- (i)** find the coordinates of C .

[3]

The line CB is extended to the point D so that B is the mid-point of CD .

- (ii)** Find the coordinates of D .

[2]

A line is drawn from D , parallel to AC , to the point $E(10, k)$ and C is joined to E .

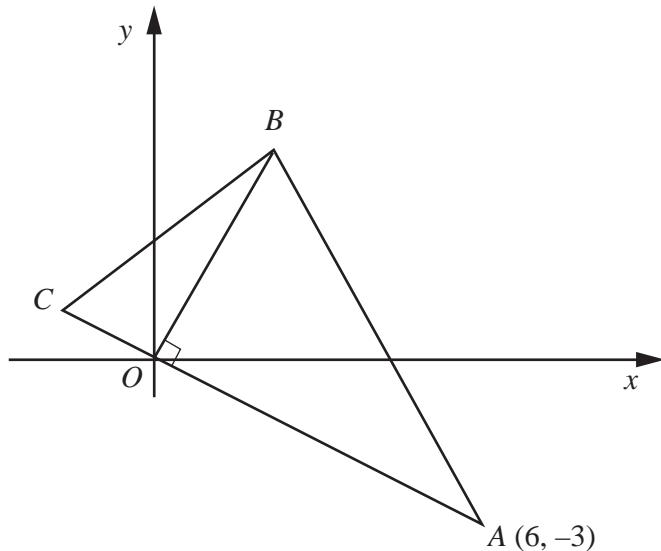
- (iii)** Find the value of k .

[3]

- (iv)** Prove that angle CED is **not** a right angle.

[2]

11 Solutions to this question by accurate drawing will not be accepted.



The diagram shows a triangle ABC in which A is the point $(6, -3)$. The line AC passes through the origin O . The line OB is perpendicular to AC .

- (i) Find the equation of OB . [2]

The area of triangle AOB is 15 units².

- (ii) Find the coordinates of B . [3]

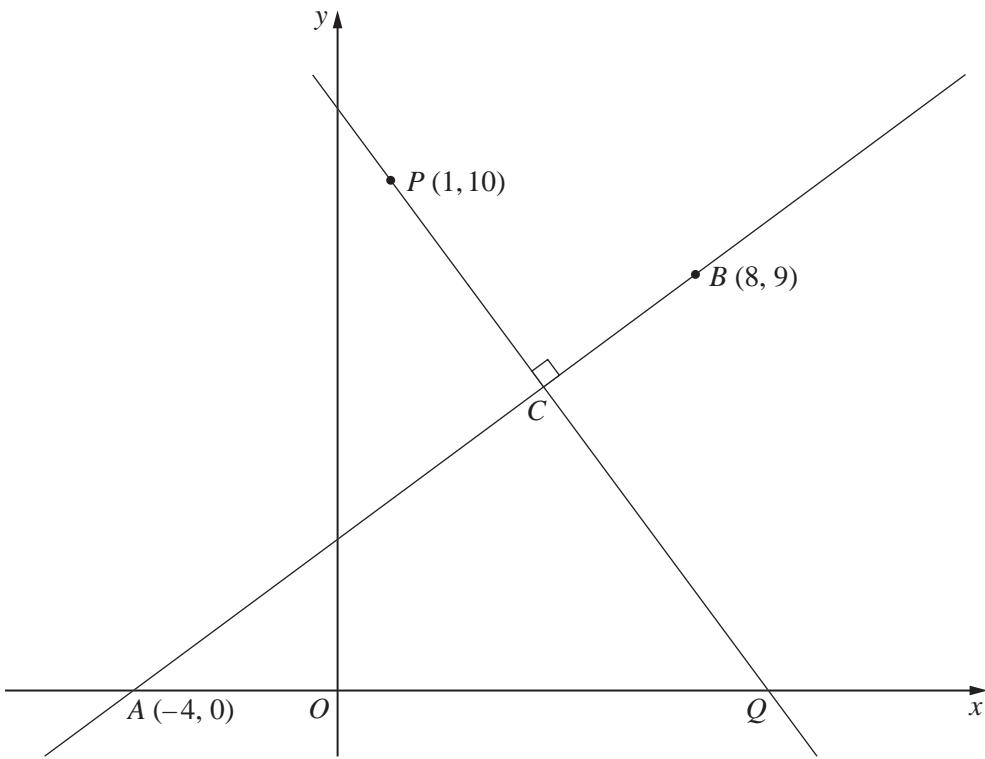
The length of AO is 3 times the length of OC .

- (iii) Find the coordinates of C . [2]

The point D is such that the quadrilateral $ABCD$ is a kite.

- (iv) Find the area of $ABCD$. [2]

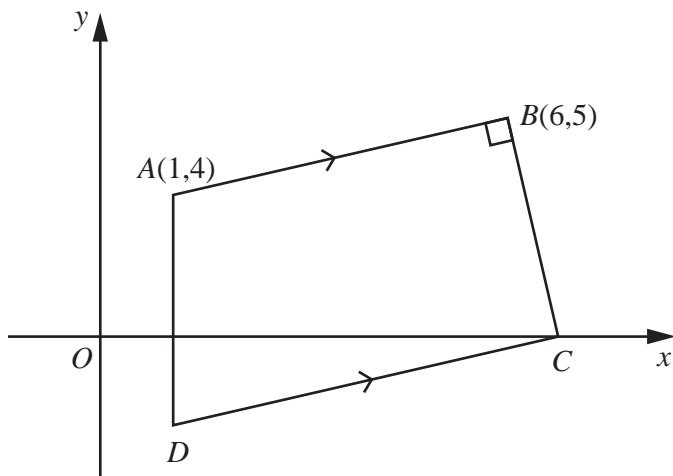
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The diagram shows the line AB passing through the points $A(-4, 0)$ and $B(8, 9)$. The line through the point $P(1, 10)$, perpendicular to AB , meets AB at C and the x -axis at Q . Find

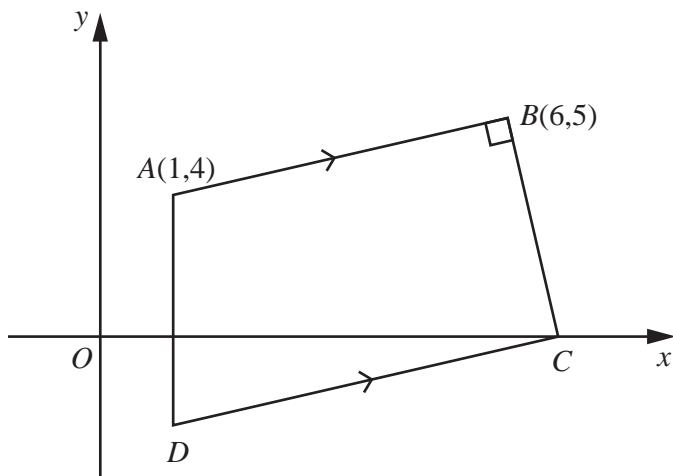
- (i) the coordinates of C and of Q , [7]
- (ii) the area of triangle ACQ . [2]

10 Solutions to this question by accurate drawing will not be accepted.



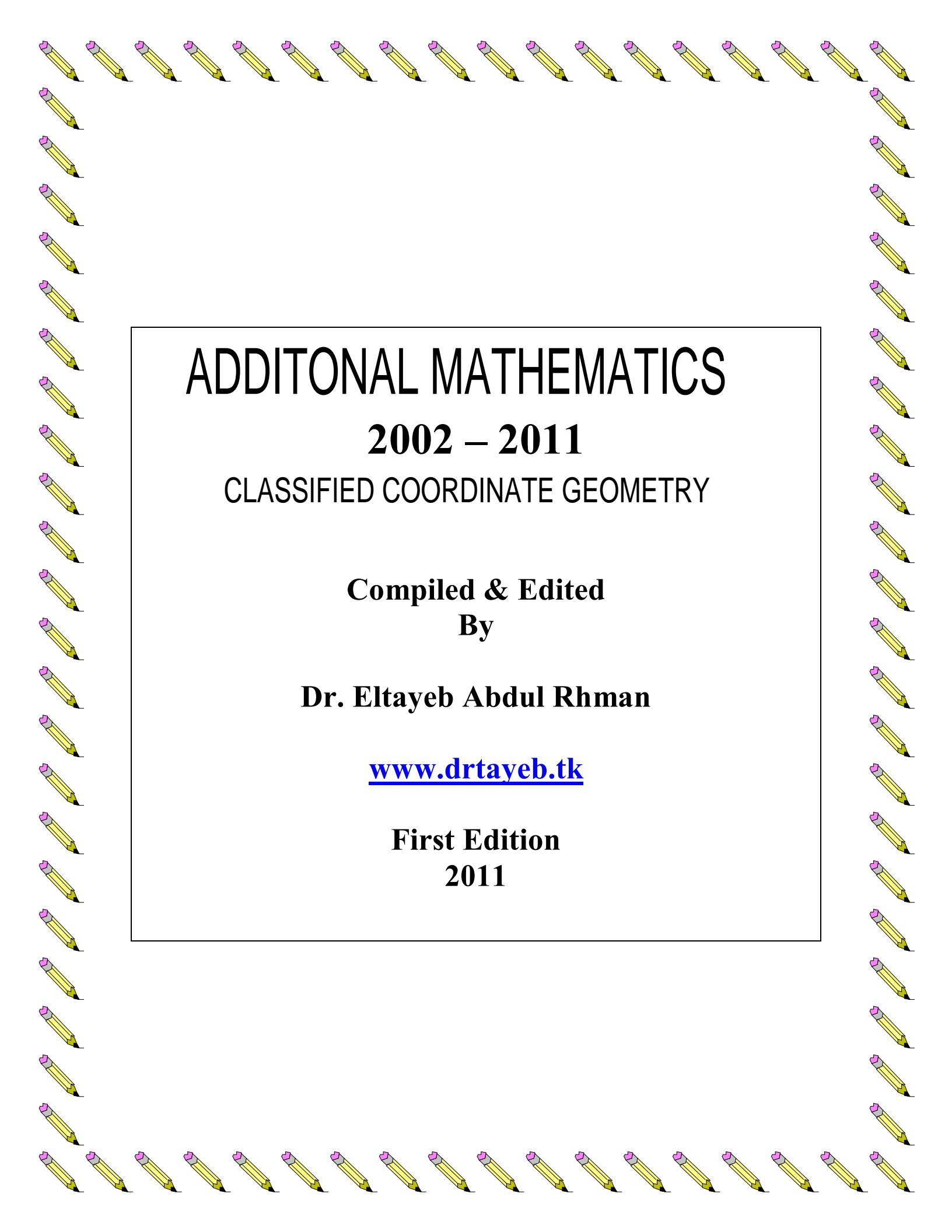
The diagram shows a quadrilateral $ABCD$ in which A is the point $(1, 4)$ and B is the point $(6, 5)$. Angle ABC is a right angle and the point C lies on the x -axis. The line AD is parallel to the y -axis and the line CD is parallel to BA . Find

- (i) the equation of the line CD , [5]
- (ii) the area of the quadrilateral $ABCD$. [4]

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The diagram shows a quadrilateral $ABCD$ in which A is the point $(1, 4)$ and B is the point $(6, 5)$. Angle ABC is a right angle and the point C lies on the x -axis. The line AD is parallel to the y -axis and the line CD is parallel to BA . Find

- (i) the equation of the line CD , [5]
- (ii) the area of the quadrilateral $ABCD$. [4]



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