

An equilateral 16-sided figure $A P A^{\prime} Q B$ $\qquad$ is formed when the square $A B C D$ is rotated $45^{\circ}$ clockwise about its centre to position $A^{\prime} B^{\prime} C^{\prime} D^{\prime}$.
$A B=12 \mathrm{~cm}$ and $A P=x \mathrm{~cm}$.
(a) (i) Use triangle $P A^{\prime} Q$ to explain why $2 x^{2}=(12-2 x)^{2}$.
(ii) Show that this simplifies to $x^{2}-24 x+72=0$.
(iii) Solve $x^{2}-24 x+72=0$. Give your answers correct to 2 decimal places.
(b) (i) Calculate the perimeter of the 16-sided figure.
(ii) Calculate the area of the 16 -sided figure.

Maria walks 10 kilometres to a waterfall at an average speed of $x$ kilometres per hour.
(a) Write down, in terms of $x$, the time taken in hours.
(b) Maria returns from the waterfall but this time she walks the 10 kilometres at an average speed of $(x+1)$ kilometres per hour. The time of the return journey is 30 minutes less than the time of the first journey.
Write down an equation in $x$ and show that it simplifies to $x^{2}+x-20=0$.
(c) Solve the equation $x^{2}+x-20=0$.
(d) Find the time Maria takes to walk to the waterfall.


A rectangular-based open box has external dimensions of $2 x \mathrm{~cm},(x+4) \mathrm{cm}$ and $(x+1) \mathrm{cm}$.
(a) (i) Write down the volume of a cuboid with these dimensions.
(ii) Expand and simplify your answer.
(b) The box is made from wood 1 cm thick.
(i) Write down the internal dimensions of the box in terms of $x$.
(ii) Find the volume of the inside of the box and show that the volume of the wood is $8 x^{2}+12 x$ cubic centimetres.
(c) The volume of the wood is $1980 \mathrm{~cm}^{3}$.
(i) Show that $2 x^{2}+3 x-495=0$ and solve this equation.
(ii) Write down the external dimensions of the box.

The length, $y$, of a solid is inversely proportional to the square of its height, $x$.
(a) Write down a general equation for $x$ and $y$.

Show that when $x=5$ and $y=4.8$ the equation becomes $x^{2} y=120$.
(b) Find $y$ when $x=2$.
(c) Find $x$ when $y=10$.
(d) Find $x$ when $y=x$.
(e) Describe exactly what happens to $y$ when $x$ is doubled.
(f) Describe exactly what happens to $x$ when $y$ is decreased by $36 \%$.
(g) Make $x$ the subject of the formula $x^{2} y=120$.

A packet of sweets contains chocolates and toffees.
(a) There are $x$ chocolates which have a total mass of 105 grams.

Write down, in terms of $x$, the mean mass of a chocolate.
(b) There are $x+4$ toffees which have a total mass of 105 grams.

Write down, in terms of $x$, the mean mass of a toffee.
(c) The difference between the two mean masses in parts (a) and (b) is 0.8 grams.

Write down an equation in $x$ and show that it simplifies to $x^{2}+4 x-525=0$.
(d) (i) Factorise $x^{2}+4 x-525$.
(ii) Write down the solutions of $x^{2}+4 x-525=0$.
(e) Write down the total number of sweets in the packet.
(f) Find the mean mass of a sweet in the packet.

2 (a) (i) Factorise $x^{2}-x-20$.
(ii) Solve the equation $x^{2}-x-20=0$.
(b) Solve the equation $3 x^{2}-2 x-2=0$.

Show all your working and give your answers correct to 2 decimal places.
(c)

$$
y=m^{2}-4 n^{2}
$$

(i) Factorise $m^{2}-4 n^{2}$.
(ii) Find the value of $y$ when $m=4.4$ and $n=2.8$.
(iii) $m=2 x+3$ and $n=x-1$.

Find $y$ in terms of $x$, in its simplest form.
(iv) Make $n$ the subject of the formula $y=m^{2}-4 n^{2}$.
(d) (i) $m^{4}-16 n^{4}$ can be written as $\left(m^{2}-k n^{2}\right)\left(m^{2}+k n^{2}\right)$.

Write down the value of $k$.
(ii) Factorise completely $m^{4} n-16 n^{5}$.

6 (a)


In triangle $A B C$, the line $B D$ is perpendicular to $A C$.
$A D=(x+6) \mathrm{cm}, D C=(x+2) \mathrm{cm}$ and the height $B D=(x+1) \mathrm{cm}$.
The area of triangle $A B C$ is $40 \mathrm{~cm}^{2}$.
(i) Show that $x^{2}+5 x-36=0$.

Answer (a)(i)
(ii) Solve the equation $x^{2}+5 x-36=0$.

$$
\begin{equation*}
\text { Answer(a)(ii) } x= \tag{2}
\end{equation*}
$$

$\qquad$

$$
\text { or } x=
$$

$\qquad$
(iii) Calculate the length of $B C$.
(b) Amira takes 9 hours 25 minutes to complete a long walk.
(i) Show that the time of 9 hours 25 minutes can be written as $\frac{113}{12}$ hours.

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Answer (b)(i)
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(ii) She walks $(3 y+2)$ kilometres at $3 \mathrm{~km} / \mathrm{h}$ and then a further $(y+4)$ kilometres at $2 \mathrm{~km} / \mathrm{h}$. Show that the total time taken is $\frac{9 y+16}{6}$ hours. Answer(b)(ii)
(iii) Solve the equation $\frac{9 y+16}{6}=\frac{113}{12}$.

$$
\text { Answer(b)(iii) } y=
$$

(iv) Calculate Amira's average speed, in kilometres per hour, for the whole walk.
$\qquad$

8 (a) $y$ is 5 less than the square of the sum of $p$ and $q$.
Write down a formula for $y$ in terms of $p$ and $q$.

$$
\text { Answer(a) } y=
$$

(b) The cost of a magazine is $\$ x$ and the cost of a newspaper is $\$(x-3)$.

The total cost of 6 magazines and 9 newspapers is $\$ 51$.
Write down and solve an equation in $x$ to find the cost of a magazine.
(c) Bus tickets cost $\$ 3$ for an adult and $\$ 2$ for a child.

There are $a$ adults and $c$ children on a bus.
The total number of people on the bus is 52 .
The total cost of the 52 tickets is $\$ 139$.
Find the number of adults and the number of children on the bus.

9 (a) The cost of a bottle of water is $\$ w$.
The cost of a bottle of juice is $\$ j$.
The total cost of 8 bottles of water and 2 bottles of juice is $\$ 12$.
The total cost of 12 bottles of water and 18 bottles of juice is $\$ 45$.
Find the cost of a bottle of water and the cost of a bottle of juice.

Answer(a) Cost of a bottle of water $=\$$
Cost of a bottle of juice $=\$$
(b) Roshni cycles 2 kilometres at $y \mathrm{~km} / \mathrm{h}$ and then runs 4 kilometres at $(y-4) \mathrm{km} / \mathrm{h}$. The whole journey takes 40 minutes.
(i) Write an equation in $y$ and show that it simplifies to

$$
y^{2}-13 y+12=0
$$ Answer(b)(i)

(ii) Factorise $y^{2}-13 y+12$.

Answer(b)(ii)
[2]
(iii) Solve the equation $y^{2}-13 y+12=0$.

$$
\begin{equation*}
\text { Answer(b)(iii) } y=\ldots . . . . . . . . . \text { or } y= \tag{1}
\end{equation*}
$$

(iv) Work out Roshni's running speed.
Answer(b)(iv) ................. km/h
(c) Solve the equation

$$
u^{2}-u-4=0 .
$$

Show all your working and give your answers correct to 2 decimal places.

2 (a) The surface area of a person's body, $A$ square metres, is given by the formula

$$
A=\sqrt{\frac{h m}{3600}}
$$

where $h$ is the height in centimetres and $m$ is the mass in kilograms.
(i) Dolores is 167 cm high and has a mass of 70 kg . Calculate the surface area of her body.
(ii) Erik has a mass of 80 kg . Find his height if $A=1.99$.
(iii) Make $h$ the subject of the formula.
(b) Factorise
(i) $x^{2}-16$,
(ii) $x^{2}-16 x$,
(iii) $x^{2}-9 x+8$.
(c) Erik runs a race at an average speed of $x \mathrm{~m} / \mathrm{s}$.

His time is $(3 x-9)$ seconds and the race distance is $\left(2 x^{2}-8\right)$ metres.
(i) Write down an equation in $x$ and show that it simplifies to

$$
\begin{equation*}
x^{2}-9 x+8=0 . \tag{2}
\end{equation*}
$$

(ii) Solve $x^{2}-9 x+8=0$.
(iii) Write down Erik's time and the race distance.

8 (a) (i) The cost of a book is $\$ x$.
Write down an expression in terms of $x$ for the number of these books which are bought for $\$ 40$.
(ii) The cost of each book is increased by $\$ 2$.

The number of books which are bought for $\$ 40$ is now one less than before.
Write down an equation in $x$ and show that it simplifies to $x^{2}+2 x-80=0$.
(iii) Solve the equation $x^{2}+2 x-80=0$.
(iv) Find the original cost of one book.
(b) Magazines cost $\$ m$ each and newspapers cost $\$ n$ each.

One magazine costs $\$ 2.55$ more than one newspaper.
The cost of two magazines is the same as the cost of five newspapers.
(i) Write down two equations in $m$ and $n$ to show this information.
(ii) Find the values of $m$ and $n$.

A sketch of the graph of the quadratic function $y=p x^{2}+q x+r$ is shown in the diagram.


The graph cuts the $x$-axis at $K$ and $L$.
The point $M$ lies on the graph and on the line of symmetry.
(a) When $p=1, \quad q=-2, \quad r=-3$, find
(i) the $y$-coordinate of the point where $x=4$,
(ii) the coordinates of $K$ and $L$,
(iii) the coordinates of $M$.
(b) Describe how the above sketch of the graph would change in each of the following cases.
(i) $p$ is negative.
(ii) $p=1, q=r=0$.
(c) Another quadratic function is $y=a x^{2}+b x+c$.
(i) Its graph passes through the origin.

Write down the value of $c$.
(ii) The graph also passes through the points $(3,0)$ and $(4,8)$. Find the values of $a$ and $b$.

(a) When the area of triangle $A B C$ is $48 \mathrm{~cm}^{2}$,
(i) show that $x^{2}+4 x-96=0$,
(ii) solve the equation $x^{2}+4 x-96=0$,
(iii) write down the length of $A B$.
(b) When $\tan y=\frac{1}{6}$, find the value of $x$.
(c) When the length of $A C$ is 9 cm ,
(i) show that $2 x^{2}+8 x-65=0$,
(ii) solve the equation $2 x^{2}+8 x-65=0$,
(Show your working and give your answers correct to 2 decimal places.)
(iii) calculate the perimeter of triangle $A B C$.


The diagram shows two rectangles $A B C D$ and $P Q R S$.
$A B=(2 x+5) \mathrm{cm}, A D=(x+3) \mathrm{cm}, P Q=(x+4) \mathrm{cm}$ and $P S=x \mathrm{~cm}$.
(a) For one value of $x$, the area of rectangle $A B C D$ is $59 \mathrm{~cm}^{2}$ more than the area of rectangle $P Q R S$.
(i) Show that $x^{2}+7 x-44=0$.
where $n$ is answer(a) positive integer and $(r)=\frac{n!}{(n-r)!r!}$.
(ii) Factorise $x^{2}+7 x-44$.

> Answer(a)(ii)
(iii) Solve the equation $x^{2}+7 x-44=0$.

$$
\operatorname{Answer}(a)(\mathrm{iii}) x=\ldots . . . . . . . . \quad \text { or } x=
$$

(iv) Calculate the size of angle $D B A$.
(b) For a different value of $x$, the rectangles $A B C D$ and $P Q R S$ are similar.
(i) Show that this value of $x$ satisfies the equation $x^{2}-2 x-12=0$. Answer(b)(i)
(ii) Solve the equation $x^{2}-2 x-12=0$, giving your answers correct to 2 decimal places.

$$
\text { Answer(b)(ii) } x=\quad . . . . . . . . . \text { or } x=
$$

(iii) Calculate the perimeter of the rectangle $P Q R S$.

9 (a) Solve the equation $\frac{m-3}{4}+\frac{m+4}{3}=-7$.

$$
\text { Answer(a) } m=
$$

(b) (i) $y=\frac{3}{x-1}-\frac{2}{x+3}$

Find the value of $y$ when $x=5$.

Answer(b)(i)
(ii) Write $\frac{3}{x-1}-\frac{2}{x+3}$ as a single fraction.
(iii) Solve the equation $\frac{3}{x-1}-\frac{2}{x+3}=\frac{1}{x}$.

Answer(b)(iii) $x=$
(c)

$$
p=\frac{t}{q-1}
$$

Find $q$ in terms of $p$ and $t$.


A farmer makes a rectangular enclosure for his animals.
He uses a wall for one side and a total of 72 metres of fencing for the other three sides.
The enclosure has width $x$ metres and area $A$ square metres.
(a) Show that $A=72 x-2 x^{2}$.

Answer (a)
(b) Factorise completely $72 x-2 x^{2}$.
(c) Complete the table for $A=72 x-2 x^{2}$.

| $x$ | 0 | 5 | 10 | 15 | 20 | 25 | 30 | 35 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $A$ | 0 | 310 | 520 |  |  | 550 | 360 |  |

(d) Draw the graph of $A=72 x-2 x^{2}$ for $0 \leqslant x \leqslant 35$ on the grid opposite.


In the right-angled triangle $A B C, A B=x \mathrm{~cm}, B C=(x+7) \mathrm{cm}$ and $A C=17 \mathrm{~cm}$.
(i) Show that $x^{2}+7 x-120=0$.

Answer(a)(i)
(ii) Factorise $x^{2}+7 x-120$.
(iii) Write down the solutions of $x^{2}+7 x-120=0$.

$$
\text { Answer(a)(iii) } x=
$$

$$
\text { or } x=
$$

(iv) Write down the length of $B C$.
(b)


The rectangle and the square shown in the diagram above have the same area.
(i) Show that $2 x^{2}-15 x-9=0$.

Answer(b)(i)
(ii) Solve the equation $2 x^{2}-15 x-9=0$.

Show all your working and give your answers correct to 2 decimal places.

$$
\text { Answer(b)(ii) } x=
$$

$\qquad$

$$
\text { or } x=
$$

$\qquad$
(iii) Calculate the perimeter of the square.

3 (a) Expand the brackets and simplify.

$$
x(x+3)+4 x(x-1)
$$

(d) Solve the equation.

$$
2 x^{2}+5 x+1=0
$$

Show all your working and give your answers correct to 2 decimal places.

> Answer(a)
(b) Simplify $\left(3 x^{3}\right)^{3}$.

> Answer(b)
(c) Factorise the following completely.
(i) $7 x^{7}+14 x^{14}$

> Answer(c)(i)
(ii) $x y+x w+2 a y+2 a w$

> Answer(c)(ii)
(iii) $4 x^{2}-49$

